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REPORT TITLE: Final Report for Abstraction and Compositionality for the Verification of Infinite-State Reactive Systems is forwarded for your information.

Sincerely,

Zohar Manna, Professor and P.I.

## DAAG 55-98-1-0471 Abstract

We describe several techniques for verifying infinite-state systems via finite-state abstractions. Diagrams are top-down property-driven abstractions, which are especially suited for compositional, assume-guarantee reasoning. Predicate abstraction uses a bottom-up approach for generating abstractions; invariant generation techniques are applied to automatically generate the required predicates. Extended finite-state abstractions allow inclusion of extra information produced by the deductive abstraction, which can be used by the model checker to reduce the number of spurious counterexamples.

These methods have been or currently are being implemented in the Stanford Temporal Prover. The methods have been applied in the analysis of a medical device.

# Final Progress Report ARO Contract DAAG 55-98-1-0471 November 30, 2001

P.I.: Prof. Zohar Manna Computer Science Department Stanford University Stanford, CA. 94305-9045

**Project Title:** Abstraction and Compositionality for the Verification of Infinite-State Reactive Systems

## **Problem Statement**

Software systems are usually *infinite-state*, since they contain system variables over unbounded domains, such as integers, lists, trees, and other data types. Most finite-state verification methods, such as model checking, cannot be applied directly to such systems. The application of temporal verification techniques to software systems is further limited by the size and complexity of the systems analyzed.

Deductive verification, which relies on general theorem-proving and user interaction, provides complete proof systems that can, in principle, prove the correctness of any property over an infinite-state system, provided the property is indeed valid for that system. However, these methods are also limited by the size and complexity of the system being analyzed, becoming much more laborious as the system complexity grows.

Verification methods analogous to those used to manage complexity in software design can be used to overcome these limitations. *Modular verification* follows the classic divide-and-conquer paradigm, where portions of a complex system are analyzed independently of each other. It holds the promise of proof reuse and the creation of libraries of verified components. *Abstraction* is based on ignoring details as much as possible, often simplifying the domain of computation of the original system. This may allow, for

instance, abstracting infinite-state systems to finite-state ones that can be more easily model checked.

## Summary of Results

## **Diagram Verification**

Diagrams are property-driven abstractions of a system: verification is only concerned with those aspects of the program that are directly related to the property, thus reducing the burden on the user. The theory of diagrams and their application in the verification of reactive, real-time and hybrid systems is described in [Sip99].

Diagrams can be applied compositionally. Diagrams are constructed and justified for each component individually, taking into account environment assumptions and restrictions. Being automata-based, these diagrams can then be composed by taking products of automata, automatically discharging the assumptions, again justified by first-order verification conditions.

Diagrams can also be used to prove safety properties of parameterized systems, that is, systems that consist of an unspecified number of identical components that interact with each other. To prove liveness properties of parameterized systems we developed the technique of dynamic induction on diagrams[MS99], which allows the verification of the property for a single component to be used to infer the validity of the property for the global system, under the appropriate ordering conditions.

Automatic generation of diagrams is hampered by the fact that the starting diagram, the automaton for the property to be proven, is exponential in the size of the formula. To alleviate this problem, we explored the use of alternating automata, which are linear in the size of the formula. In [MS00] we demonstrated the use of alternating automata in the deductive verification of safety properties. We are currently extending this to the deductive verification of progress properties. Although generally applicable, this method appears to be especially suitable for assume-guarantee properties.

## Program Abstraction by Invariant Generation

In [CU98] we presented a two-phase approach to program abstraction. It first uses theorem proving to construct a finite-state abstraction of an infinite-state program, and then finite-state analysis to compute the reachable states of the abstraction. This set of reachable abstract states is then used to verify

temporal properties of the concrete system. This method, while highly automated, requires user guidance in the form of a finite set of atomic assertions over the variables of the concrete program.

Invariant generation can be used to generate these abstractions automatically. We use the decidable theory of linear inequalities as a basis to discover program invariants. Our approach is to symbolically simulate the program for a number of program steps, representing them by linear systems, and then search for invariants among the common consequences of these systems. The advantage of this deductive variant of linear invariant generation is its generalizability: it admits the presence of disequalities and strict inequalities, thereby enabling the generation of more precise invariants in, for example, the branches of conditional statements.

We have also used this technique to automatically generate ranking functions for establishing loop termination [CS01]. The technique reduces the search for linear ranking functions to the problem of finding certain consequences of two linear systems – one approximating the transition relation around the loop and the other approximating the states reachable while in the loop. By manipulating these systems, the algorithm isolates those consequences that define linear ranking functions.

#### **Extended Finite-state Abstraction**

Many deductive and deductive-algorithmic verification methods explicitly or implicitly construct finite-state system abstractions, which are explicitly or implicitly model checked. We show how such abstractions can be represented, combined and model checked in a general way. For this, we define a class of extended finite-state abstractions, and present an algorithmic model checking procedure for them. This procedure uses all the information produced by the deductive algorithmic methods, in a finite-state format that can be easily and incrementally combined. Besides a standard ∀CTL\*-preserving safety component, the extended abstractions include extra bounds on fair transitions, well-founded orders, and constrained transition relations for checking existential properties or the generation of LTL counterexamples. This approach minimizes the need for user interaction and maximizes the impact of the available automated deduction and model checking tools. Once proved, verification conditions are re-used as much as possible, leaving the temporal and combinatorial reasoning to automatic tools. The method is described in detail in [MSU99, Uri00, Uri01].

## Applications

In the final year of the contract we have started to apply above methods to the analysis of a medical device: a computer-assisted resuscitation device developed by the Walter Reed Army Institute of Research (WRAIR). Based on detailed tagged requirements developed by physicians at WRAIR, a clocked transition system was created to model the system. The system, consisting of some 400 transitions, was divided into modules, interacting by shared variables, and provided with environment assumptions both on timing behavior and data modification. Abstraction techniques and modular reasoning were used to check the system for infinite loops. Further analysis of this system is planned when funding is secured.

#### Implementation

The modular verification techniques proposed in [FMS98, BMSU01] were implemented in STeP (Stanford Temporal Prover) for reactive and real-time systems. We are currently implementing these methods for hybrid systems. An overview of the STeP system can be found in [BBC<sup>+</sup>00].

Except for the first-order theorem-proving component, STeP has been reimplemented in Java, with the objective to obtain a more modular architecture that is easily extensible with new methods and computational models. It allows for quick experimentation to evaluate new techniques.

## **Publications**

#### Journal papers

 Nikolaj S. Bjørner and Anca Browne, Michael Colón, Bernd Finkbeiner, Zohar Manna, Henny B. Sipma, Tomás E. Uribe, Verifying Temporal Properties of Reactive Systems: A STeP Tutorial. Formal Methods in System Design, Vol 16, June 2000.

#### Conference papers

 Anca Browne, Henny Sipma, and Ting Zhang, Linking STeP with SPIN. In SPIN Model Checking and Software Verification, 7th International SPIN Workshop, vol 1885 of Lecture Notes in Computer Science, pages 181–186. Springer Verlag 2000.

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#### List of Scientific Personnel

Scientific personnel who participated in the project:

- Faculty: Prof. Zohar Manna
- Scientific Personnel: Dr. Henny B. Sipma, Anca Browne
- Graduate students: Michael Colon, Bernd Finkbeiner, Henny Sipma, Tomas Uribe, Ting Zhang
- Visitors: Prof. Saddek Bensalem, VERIMAG, France; Arnab Ray, SUNY Stony Brook.

#### Graduated Ph.D. students:

- Henny Sipma February 1999. Thesis: Diagram-Based verification of reactive, real-time and hybrid systems
- Tomás E. Uribe, December 1998. Thesis: Abstraction-based Deductive-Algorithmic Verification of Reactive Systems.

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